P5 Box2D Physics Tutorial
© by Robert Cook at professorcook.org

**Foreword:** The tutorial is the Physics chapter from *Introduction to Programming with JavaScript, P5 and Processing* by Robert Cook on amazon.com. Please send any corrections or suggestions to kindlecbook@gmail.com. Thank you for your purchase. The code in the tutorial can be reused under the [M.I.T. license](https://github.com/magebuild/PhysicsEngine/blob/master/LICENSE).

---

Skip to the Physics Section if you already understand Fiddles and debugging. One of the nice features of the web IDE JSFiddle.net is that JavaScript can be entered directly without worrying about `<script>` tags. We will take advantage of this feature in the tutorial to test additional JavaScript features.

Click the JSFIDDLE text in the application to create a new JavaScript Fiddle. Clicking Save creates a new web document that contains your code. The result can then be accessed worldwide. JSFiddle saves all versions of your code until you are satisfied with the result. Then, click Update and SetAsBase to make a particular version the default for that URL. JSFiddle generates a unique URL for every Fiddle. By clicking FiddleOptions, you can give your Fiddle a human-sensible name, which other people can access by using the URL jsfiddle.net/user/bobcook.

**JavaScript JSFiddle Window**
http://jsfiddle.net/bobcook/3eurmvjd/

---

Remember "**Processing** is an open source programming language and integrated development environment (IDE) built for the electronic arts, new media art, and visual design communities with the purpose of teaching the fundamentals of computer programming in a visual context, and
to serve as the foundation for electronic sketchbooks." P5 is the pure JavaScript implementation of Processing.

The First P5 JavaScript Program
http://jsfiddle.net/bobcook/na01uv1h

JavaScript Libraries

Navigate to the P5 example or create your own by copying the code (select the "No wrap - in <body> option). Another rule of programming is "Copy code that works, then modify it one step at a time to satisfy your requirements". Of course, be sure to abide by copyright restrictions.

Since programs have lots of white space and since libraries can be quite large, there are applications that "minify" JavaScript code to make it more compact. Thus, "p5.min.js" is a min-sized version of the P5 library.

The HTML in the example illustrates one way to refer to a library in JSFiddle. JSFiddle provides a second library option that is useful when multiple libraries are required.

Click FrameWorks&Extensions. The Figure does not show it, but select No-Library (pure JS) and NoWrap - in <head> as options. Also, be aware that the external URL should have an http:// prefix. You can "Fork", or copy, this example to create your own P5 Fiddles.

JSFiddle Library Option
http://jsfiddle.net/bobcook/mnfytay6
Vector Class

One of the basic building blocks for programming motion is the vector, which is named for the Greek mathematician Euclid and is also known as a geometric vector. A vector defines a magnitude (or length) and a direction in a Cartesian coordinate system graph. A vector is usually drawn as an arrow. The magnitude of the vector is its length while its tip indicates the direction.

A Vector

Obviously, a line requires a point at each end; however, the length of a line and its direction can be represented by translating the line's starting point to the origin (0,0). As a result, a vector can be described by its end point only (a single xy pair of values). In physics, velocity is a vector that can be applied to a point to change its location.
Another term from physics is **acceleration**, which is the addition of a vector to the velocity of a point. The Earth's standard acceleration due to gravity is $g = 9.80665 \text{ m/s}^2$ (32.1740 ft/s$^2$). Other physical forces (wind, lift, drag, friction, buoyancy, magnetism etc.) can also be coded as vectors.

An operator, such as vector addition, is just the application of a change in location. For example, go to the refrigerator in the real world might translate into 6 steps east then 9 steps north in the vector world. Similarly, vector subtraction would simply reverse the path from the refrigerator so that we ended up where we started. In the Figure, $(a+b)-b$ is the vector $a$. Vector multiplication scales a vector by an x-direction multiple and a y-direction multiple.

A common human use of vectors is a list of driving directions from one city to another. Each segment is a direction/magnitude vector. How does the program calculate the distance?

**Driving Directions**
The length, or magnitude, of a vector is calculated using geometric principles that have existed for thousands of years. Even cave people had to guess how tall a tree was so it would not crush anything when felled.

A circle represents a 360 degree arc that can be divided into four 90 degree quadrants (X Y, -X Y, X -Y, -X -Y) on a Cartesian graph. In most mathematical work, angles are typically measured in radians rather than degrees.

A right triangle is a three-sided figure in which one angle is a right angle (that is, a 90-degree angle). The relation between the sides and angles of a right triangle is the basis for trigonometry.

The side opposite the right angle is called the hypotenuse (side c in the figure). The small square at the right angle is the typical symbol used to denote that an angle is 90°.
In the Figure, (b,a) is the vector notation for c. We wish to calculate the length of c. The Pythagorean Theorem—or Pythagoras' theorem—is a relation in geometry among the three sides of a right triangle. It states that the square of the length of the hypotenuse (the side opposite the right angle) is equal to the sum of the squares of the lengths of the other two sides. The theorem can be written as an equation relating the lengths of the sides a, b and c, often called the Pythagorean equation: \( a^2 + b^2 = c^2 \). The Pythagorean theorem is named after the Greek mathematician Pythagoras (ca. 570 BC—ca. 495 BC), who by tradition is credited with its proof. The length of a vector (b, a) is calculated as \( \sqrt{a^2 + b^2} \).

Observe that in the right triangle in the Figure, there are two angles that are unknown. Typical problems that have challenged humans for thousands of years are to be given lengths and to be asked for angles or to be given an angle and asked for lengths. Thus, the science of trigonometry was born. Three of the main functions in trigonometry are sine, cosine and tangent. They are all based on analysis of a right triangle.

**Right Triangle Side Names**
Remember that there are two angles of interest. Either angle can be calculated based on a ratio of side lengths. The **hypotenuse** is always the side opposite the right angle and is the longest side. The **adjacent** side forms the angle of interest together with the hypotenuse. The **opposite** side is the line connecting the hypotenuse to the adjacent side. The ratios are calculated as listed in the table. The mnemonic to help you remember the definitions is **soh cah toa**. Given the side lengths, the two angles can be computed; given the angles, the two side lengths can be computed.

<table>
<thead>
<tr>
<th>Function</th>
<th>Ratio</th>
</tr>
</thead>
<tbody>
<tr>
<td>sine(angle in radians)</td>
<td>Opposite / Hypotenuse</td>
</tr>
<tr>
<td>cosine(angle in radians)</td>
<td>Adjacent / Hypotenuse</td>
</tr>
<tr>
<td>tangent(angle in radians)</td>
<td>Opposite / Adjacent</td>
</tr>
<tr>
<td>tangent(angle in radians)</td>
<td>sine(angle) / cosine(angle)</td>
</tr>
<tr>
<td>angle in radians</td>
<td>arc cos(Adjacent / Hypotenuse)</td>
</tr>
</tbody>
</table>

There are an infinite number of vectors that have the same direction, but different lengths (1,1) (2,2) (0.8,0.8) etc. It would be useful if we could represent all of the vectors that point in the same direction as just one vector. In math, this goal is termed a **canonical representation** or a **normal form**. For vectors, the canonical representation of all vectors with the same direction is called a **unit vector**. It should be intuitive that if all the lengths are different but the direction is the same, the unit representation for a vector can be calculated by dividing by its length, which results in a length of one.

In the sine/cosine table, if the hypotenuse's length is one, the sine and cosine give the length of the Opposite and Adjacent sides directly. Observe that a unit vector has a length of one. As a result, the distance from the hypotenuse to the X or Y axis can be calculated. The relationship between a unit vector and side lengths is frequently depicted as a unit circle, which is shown next. The length of the Opposite side is 0.899/1 and the length of the adjacent side is 0.438/1 for an angle of 64 degrees.

**Unit Vector**
The JavaScript math library includes the described trigonometric functions in addition to the inverse functions, such as Math.acos(), which will invert a cosine result to its argument angle (in radians).

Another useful geometric concept is the **dot product**, which is used in graphics as well as in other fields, such as mechanics. The dot product \((v1 \cdot v2)\) of two vectors is the cosine of the angle between them, multiplied by the lengths of the vectors, \(v1\) and \(v2\). So, you can easily calculate the cosine of the angle by either making sure that the two vectors are both of length one, or by dividing the dot product by the lengths. The actual angle between the two vectors can be determined by applying Math.acos to the cosine result.

**Angle Between Two Vectors**

\[
\text{DotProduct}(v1,v2) = \cos(\text{angle}) \times \text{length}(v1) \times \text{length}(v2)
\]

\[
\cos(\text{angle}) = \frac{\text{DotProduct}(v1,v2)}{(\text{length}(v1) \times \text{length}(v2))}
\]

It has been proven (see Wikipedia) that the geometric definition of the dot product is equivalent to the algebraic definition. Since the algebraic definition is more efficient to calculate, it is the one implemented in the Vector class.

```javascript
function dot(v1, v2) {
    return v1.x*v2.x + v1.y*v2.y;
}

dot( (.438,0), (.438,.899) ) = \text{adjacent} \times \text{hypotenuse} = (.438*.438 + 0*.899) / (.438 \times 1) = .438
```
Math.acos(.438) = 1.117 radians
degrees(1.117) = 63.999 degrees

The dot product values range from 1 to -1. If the two input vectors are pointing in the same direction, then the return value will be 1. If the two input vectors are pointing in opposite directions, then the return value will be -1. If the two input vectors are at right angles, then the return value will be 0. To solve for angle theta, use the geometric dot product formula. The Math.acos() function can be used to calculate the angle between two vectors by dividing the dot product of two vectors by their lengths.

**Dot Product**

\[ A \cdot B = |A| |B| \cos \theta \]

![Dot Product Diagram](image)

The cross product is another geometric concept to discuss before proceeding to the design of the Vector class. The **cross product** of two vectors \((v1 \times v2)\) is another vector that is at right angles to both. It has uses in three dimensions that we will not be discussing.

We are interested in the cross product in two dimensions because its magnitude \(c_z\) can be interpreted as the area of a parallelogram having side lengths of only \(v1\) and \(v2\). Given two unit vectors, their cross product has a magnitude of 1 if the two are perpendicular and a magnitude of zero if the two are parallel.

**Cross Product**
In physics and in gaming, lots of things (balls, light, cars, bullets) bounce off of other things. There is a law for that which states that the angle of reflection is equal to the angle of incidence with respect to a surface's normal vector. Basically, a ball bounces off a surface at the same angle at which it arrived. The normal of a flat surface is a vector that is perpendicular to it. Note that a "normal" vector is a different concept than normalizing a vector.

**Angle of Reflection**
The P5 library implements a vector class, which includes all of the methods discussed. The following table summarizes the design of the Vector class.

**P5 Vector Methods**

<table>
<thead>
<tr>
<th>Method</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td><code>createVector(x, y [,z])</code></td>
<td>Creates a new p5.Vector instance.</td>
</tr>
<tr>
<td><code>new p5.Vector(x, y [,z])</code></td>
<td>Creates a new p5.Vector instance.</td>
</tr>
<tr>
<td><code>v.add(x, y)</code></td>
<td>Adds x, y, and z components to a vector, adds one vector to another, or adds two independent vectors together. The version of the method that adds two vectors together is a static method (p5.Vector.add) and returns a p5.Vector, the others act directly on the vector.</td>
</tr>
<tr>
<td><code>v.add(v2)</code></td>
<td></td>
</tr>
<tr>
<td><code>v.array()</code></td>
<td>Return a representation of this vector as a float array.</td>
</tr>
<tr>
<td><code>v.copy()</code></td>
<td>Gets a copy of the vector, returns a p5.Vector object.</td>
</tr>
<tr>
<td><code>v.cross(v2)</code></td>
<td>Calculates and returns a vector composed of the cross product between two vectors. Both the static and non static methods return a new p5.Vector.</td>
</tr>
<tr>
<td><code>v.dist(v2)</code></td>
<td>Calculates the Euclidean distance between two points (considering a point as a vector object).</td>
</tr>
<tr>
<td><code>v.div(scale)</code></td>
<td>Divide the vector by a scalar. The static version of this method creates a new p5.Vector while the non static version acts on the vector directly.</td>
</tr>
<tr>
<td><code>v.dot(v2)</code></td>
<td>Calculates the dot product of two vectors. The version of the method that computes the dot product of two independent vectors is a static method.</td>
</tr>
<tr>
<td><code>v.equals(v2)</code></td>
<td>Equality check against a p5.Vector.</td>
</tr>
<tr>
<td>Method</td>
<td>Description</td>
</tr>
<tr>
<td>--------</td>
<td>-------------</td>
</tr>
<tr>
<td><code>p5.Vector.fromAngle(radians)</code></td>
<td>Make a new 2D unit vector from an angle.</td>
</tr>
<tr>
<td><code>v.heading()</code></td>
<td>Calculate the angle of rotation for this vector (only 2D vectors).</td>
</tr>
<tr>
<td><code>v.lerp(v2, percent)</code></td>
<td>Linear interpolate the vector to another vector.</td>
</tr>
<tr>
<td><code>v.limit(max)</code></td>
<td>Limit the magnitude of this vector to the value used for the <code>max</code> parameter.</td>
</tr>
<tr>
<td><code>v.mag()</code></td>
<td>Calculates the magnitude (length) of the vector and returns the result as a float (this is simply the equation (\sqrt{x^2 + y^2 + z^2})).</td>
</tr>
<tr>
<td><code>v.magSq()</code></td>
<td>Calculates the squared magnitude of the vector and returns the result as a float (this is simply the equation (x^2 + y^2 + z^2)). Faster if the real length is not required in the case of comparing vector lengths, etc.</td>
</tr>
<tr>
<td><code>v.mult(s)</code></td>
<td>Multiply the vector by a scalar. The static version of this method creates a new <code>p5.Vector</code> while the non static version acts on the vector directly.</td>
</tr>
<tr>
<td><code>v.normalize()</code></td>
<td>Normalize the vector to length 1 (make it a unit vector).</td>
</tr>
<tr>
<td><code>p5.Vector.random2D()</code></td>
<td>Make a new 2D unit vector from a random angle.</td>
</tr>
<tr>
<td><code>p5.Vector.random3D()</code></td>
<td>Make a new random 3D unit vector.</td>
</tr>
<tr>
<td><code>v.rotate(radians)</code></td>
<td>Rotate the vector by an angle (only 2D vectors), magnitude remains the same.</td>
</tr>
<tr>
<td><code>v.set(x,y, [z])</code></td>
<td>Sets the x, y, and z component of the vector using two or three separate variables, the data from a <code>p5.Vector</code>, or the values from a float array.</td>
</tr>
<tr>
<td><code>v.setMag(len)</code></td>
<td>Set the magnitude of this vector to the value used for the <code>len</code> parameter.</td>
</tr>
<tr>
<td><code>v.sub(x,y)</code></td>
<td>Subtracts x, y, and z components from a vector, subtracts one vector from another, or subtracts two independent vectors. The version of the method that subtracts two vectors is a static method and returns a <code>p5.Vector</code>, the other acts directly on the vector.</td>
</tr>
</tbody>
</table>

**Examples**

http://jsfiddle.net/bobcook/5n0nbr9y

<table>
<thead>
<tr>
<th>Code</th>
<th>Output</th>
</tr>
</thead>
</table>
| ```javascript
function setup() {
  createCanvas(600, 400);
  var v = new p5.Vector(4,5);
  out(v);
  out(v.add(1,2));
  out(v.add(v));
} ```  
| v=4 5  
v+1,2 = 5 7  
v+v = 10 14 |
```javascript
out(p5.Vector.add(v, v));
var y = createVector(0, 4);
var x = createVector(10, 0);
var r = p5.Vector.angleBetween(x, y);
out(degrees(r));
out(v.array().length);
var r = createVector(0, 0);
// r = x.copy();
r.y = 9;
out(x);
out(r);
out(x.cross(y));
out(x.dist(y));
out(v.div(2));
out(x.dot(y));
// out(x.equals(y));
out(p5.Vector.fromAngle(PI/2));
out(x.heading());
out(r.lerp(3, 3, 0, 0.5));
out(r);
out(x);
out(y);
out(x.lerp(x, y, 0.5));
out(x);
out(x.limit(2));
out(x.mag());
out(x.magSq());
out(x.mult(2));
out(x.normalize());
out(p5.Vector.random2D());
out(p5.Vector.random3D().z);
out(x.rotate(PI/3));
out(x.set(3, 4));
out(x.setMag(6));
out(x.sub(1, 1));
out(x.sub(y));
}
```

Vector Demonstration

One of the traditional demonstrations for the utility of a Vector class is moving object collision. The sample code implements circle collision because the intersection test is trivial. Two circles intersect if the distance between the centers is less than the sum of the radii.
The main code generates N instances of the Circle class. One complication was that the collision response did not handle circles that were created on top of each other. As a result, the generator code in "setup" had to delete a Circle if it overlapped another and try again.

To add interest, colliding balls turn red and we have added a sound (beep MP3 file). At each "step", every ball must check for a wall collision. Also, each ball must check to see if it is colliding with any other balls. This an expensive test, that at its simplest, requires N balls to check N-1 other balls. This is N^2 operations. There are much better algorithms for collision testing. We opt for simplicity over speed. Also, collision testing gets more complicated for irregular figures.

Bouncing Circles
1. The first step was to modify the Circle class to store the xy position as a vector. Next, the "setup" method was modified to generate Circles at random positions. The location range is inset by the largest radius so that no Circle overlaps an edge of the canvas. We also added a "velocity" property to each Circle, but did not use it immediately as step-wise refinement dictated that the new vector/drawing code be tested first.

The "sound" library can be downloaded from the P5 web site, which also has numerous usage examples. Be sure to add the following tag to index.html.

```html
<script language="javascript" type="text/javascript" src="../p5.sound.js"></script>
```

```javascript
var balls = [];
var N = 13;
var beep;
function preload() {
  beep=loadSound("assets/beep.mp3");
}
function setup() {
  createCanvas(400, 400);
  start: for (var i = 1; i <= N; i++) {
    var c = new Circle(
```
random(15, width - 15),
random(15, height - 15),
random(4, 15));
c.velocity = p5.Vector.random2D().mult(4);
for (var j = 0; j < balls.length; j++) {
  if (c.isIntersecting(balls[j])) continue start;
} balls.push(c);
} //for i
} //setup

2. The next step was to loop through the "balls" array incrementing the position by the velocity.

    for (var i = 0; i < balls.length; i++) {
      balls[i].xy.add(balls[i].velocity);
    }

3. Then the xy position of each ball had to be tested for intersection with a canvas edge. By testing x and y collisions separately, the corner-collision test is included for free. If a collision occurs, a beep sound is played. Herein occurred the first bug. It turns out that sounds are queued so that if five collisions are detected in a second, the beeps will still be playing long after the circles have gone their separate ways. The solution was to only play a new beep if an old one had stopped playing.

function draw() {
  background(51);
  var xy, beeper = false;
  for (var i = 0; i < balls.length; i++) {
    balls[i].xy.add(balls[i].velocity);
  }
  for (var i = 0; i < balls.length; i++) {
    var xy=balls[i].xy;
    var collision = false;
    if (xy.x < balls[i].r || xy.x > (width - balls[i].r)) {
      collision = true;
      balls[i].velocity.x = -balls[i].velocity.x;
    }
    if (xy.y < balls[i].r || xy.y > (height - balls[i].r)) {
      collision = true;
      balls[i].velocity.y = -balls[i].velocity.y;
    }
    collision = collision || balls[i].testAndBounce(balls);  
    if (collision) {
      beeper = true;
      balls[i].xy.add(balls[i].velocity);
      fill(255, 0, 0);
    } else {  

```javascript
  balls[i].xy = xy;
  fill(255);
}
ellipse(balls[i].xy.x, balls[i].xy.y, balls[i].r*2, balls[i].r*2);
} //for i
if (beeper && !beep.isPlaying()) beep.play();
}

4. The final step was to implement the "testAndBounce" method, which checks for a ball collision against an array of balls. If a collision is detected, the velocity is modified in the opposite direction proportional to the strength of the collision. For example, a head-on crash is more powerful than a glancing blow by two circles heading in the same direction.

Circle.prototype.testAndBounce = function(circles) {
  for (var i=0; i<circles.length; i++) {
    var b = circles[i]; //reference, not copy
    if (b == this) continue;
    if (b.xy.dist(this.xy) > (this.r+b.r)) continue;
    var dif = p5.Vector.sub(this.xy, b.xy);
    dif.normalize();
    var dot = dif.dot(this.velocity)*-2;
    dif.mult(dot);
    this.velocity.add(dif);
    return true;
  } //for i
  return false;
}
```

---

**Debugging State**

While in theory a programmer is supposed to keep track of program state (variables and their values), in practice most of us lose track if there are more than a few variables. I am sure that you have already made a mistake in your code and discovered that the Fiddle does not run. That is not very helpful.

Luckily, many web browsers include JavaScript debuggers. Debuggers support two main features. First, it is very easy to examine program state. Second, it is possible to set a breakpoint in a program and the to "step" execution by one line at a time. When program execution reaches a line that is a breakpoint, the debugger halts execution so that the programmer can view the variables and their values.

Remember determinism. Given a program's state and a line of code, be able to determine the result. At a breakpoint, you can view the state, then you figure out what the result
should be for the current statement, then you step the code one line forward and compare the actual result with your assumption.

Firefox Debugging

We recommend the Firefox debugger, which is available free at mozilla.org. To use the Firefox debugger, you need to create a web site on the desktop. You can also debug a Fiddle online but often all the JavaScript running the environment can obscure the details of your code.

Getting Started

5. Download Firefox from Mozilla.org, if needed.
6. Create a directory on the Desktop. I named mine "p5".
7. Create a directory in p5 called "test".
8. Create a text file named "index.html" for your new web site. Be warned that many text editors, such as Microsoft Word, add hidden formatting characters that will make a file unusable as a web page, even though the text "looks fine" in the editor. The "index.html" file must be "plain text", which usually has a ".txt" suffix. Some File Manager applications hide file suffixes so you might end up with a name like index.html.rtf and not know it. Examine the File Manager options to turn on suffix display. Copy the following HTML, which is also posted at JSFiddle.

```html
<html>
<head>
  <script language="javascript" type="text/javascript"
src="http://cdnjs.cloudflare.com/ajax/libs/p5.js/0.4.4/p5.min.js"></script>
  <script language="javascript"
src="http://cdnjs.cloudflare.com/ajax/libs/p5.js/0.4.4/addons/p5.dom.min.js"></script>
  <script language="javascript"
src="http://cdnjs.cloudflare.com/ajax/libs/p5.js/0.4.4/addons/p5.sound.min.js"></script>
  <script language="javascript" type="text/javascript" src="sketch.js"></script>
  <style> body {padding: 0; margin: 0;}</style>
</head>

<body>
</body>
</html>
```

9. The HTML loads the P5 libraries from a public web site then loads your JavaScript code from a file in the test directory named "sketch.js". Create a text file named "sketch.js" in the test directory. Copy the JavaScript code for the projectile from the Fiddle version.
10. Double-click on the index.html name. If Firefox is not your default browser, you may need to right-click and select execution with Firefox. The program should run and display the parabolic trajectory arc. Click on the triple-line icon in the upper right to display Developer options, then click Developer.

**Firefox Developer Options**

11. Select the "Page Source" option. The HTML source for index.html is displayed. This is a great option to know about as it can be used on any web page to examine how it works.
12. Next, select the Debugger option. The following panel is added to the bottom of the screen.
Firefox Console

Before introducing debugging, we need to discuss the benefits of the Firefox console. Earlier examples used alert and document.write to display program output. By using Firefox's console, two more options are available. JavaScript implements a `console.log(list)` function and P5 implements a `print(list)` function.

Remember the P5 `draw()` function is invoked sixty times per second. When debugging display functions, set the frame rate to one.

1. Double-click on index.html. Use the previous instructions to display the Console panel. Click the Console tab, then the Logging tab, then click the "reload page" icon in the address bar.
2. TIP: For accelerated development, keep sketch.js open in an editor. As errors are discovered, fix them in the file. Next, select File/Save instead of closing the editor and double-clicking index.html. Just click the browser's Reload icon in the tool bar and the sketch will be re-executed with the updated code.

3. The next Figure shows a sample error message. Error messages are often unclear. Clicking on the sketch.js:8:15 hyperlink on the right will highlight text within one line of the error. From that point, you are on your own to track down what you did wrong.

    function setup() {

Firefox Debugger
1. Select the Debugger tab next to Console, then click sketch.js under the Sources tab. Next, click the || icon right above the Sources tab to stop the program. There are no syntax errors; the program just does not work. Then, click to the left of line 20 in the blank column to set a breakpoint (a blue circle). Breakpoints can be removed by just clicking them a second time. Now click the right-pointing triangle above the Sources tab to execute the program. The program stops at line 20 and highlights with a right-pointing green arrow.

2. At this point the user has a number of debugging options.
   a. Highlight any global variables or any variables local to the function, hover the mouse, and the value of the variable will be displayed. If everything looks ok, the breakpoint can be removed. Click the right-pointing triangle to continue program execution. There are also three icons above the Sources/CallStack tabs that provide additional execution options.
   b. Click the StepOver icon to execute one statement at a time. The term "Over" means that if the statement is a function reference, execution will enter the function but will not "break" until control has returned to the next line.
   c. Click the StepInto icon to execute one statement at a time. The term "Into" means that if the statement is a function reference, execution will enter the function and step to its next line.
   d. The StepOut icon is chosen in situations in which a function has been checked out to be correct but execution has not yet reached the end of the function. It can be tedious to StepOver multiple statements that are not of interest. The StepOut option defers the next "break" until the current function has exited.

3. Click the StepInto icon to trace into the "update" function. The previous Figure shows that I highlighted the "angle" variable to check its value.

4. Next, StepOver until line 29 is reached. The far-right column shows the names and values of all the local variables. Notice that x and y have the value NotANumber, but that cannot be right because width, r and x0 were initialized earlier. Weren't they? These steps illustrate how I found and fixed my error in one of my sketches.
PHYSICS FOR FUN

Introduction

Hopefully the vector math and geometry examples that have been introduced so far were sufficient to convince you that traditional "stuffy" subjects can enable cool programs in the world of JavaScript. In this tutorial we do not introduce new programming concepts, rather we introduce you to game physics simply because it is fun to play with!

Box2D Physics Library
The Box2D physics engine (box2d.org), which was originally written in platform-independent C++, has also been ported to JavaScript. The version (box2d-html5) that is used in the examples is the same as that used in the Nature of Code examples by Daniel Shiffman.


Box2D was first released as a demonstration engine to accompany a physics presentation given by Erin Catto at the 2006 Game Developers Conference. The code was posted as an open-source release in 2007.

Box2D implements a constrained, rigid-body simulation that can model bodies composed of edges, rectangles, convex polygons (no concave angles) or circle shapes. Rigid bodies never deform; their perimeter always remains exactly the same no matter what forces are applied. A single polygon is **RESTRICTED** to a maximum of eight vertices.

Bodies are connected together with joints and acted upon by forces. Concave polygons can be implemented by joining multiple convex pieces. The shapes are used only in the physics simulation; they define the boundary of sprites and static barriers, such as buildings, roads, or cliffs. When a program draws a body, the figure has no restrictions. It can be an image or an animation. Remember that the physics shapes are chosen to be a close approximation to the boundary of what is drawn. For debugging, the physics library includes a default drawing routine for all body types.

Box2D was designed to utilize the standard physics units of meters/kilograms/seconds. The simulation algorithms are optimized for object sizes ranging from 0.1m (a grape) to 10 meters (a school bus). The API provides a scale function (up to about 30) to go larger, but not smaller, which translates from about 3 pixels to 300.

The engine also integrates gravity, density, friction, and bouncing (termed restitution) calculations as well as collision detection. Gravity is an acceleration vector so objects can fall up, down, sideways, or not all all. Density determines the mass of a body (mass equals density*area). Friction regulates two bodies that are in sliding contact.
The Box2D user controls the physics engine by creating objects with numerical properties. The engine then evaluates a complicated series of formulas that approximate the objects' behavior in the physical world. Be aware that this is an imperfect system. Sometimes the results can be very strange. More often, the results are impressive. Be prepared to experiment with the parameters to achieve your goals. Remember you are using physics, not learning the details from a physics textbook. People drive cars, but not everyone can replace brake linings.

**Physics Bodies**

Remember that acceleration is the change in an object's velocity over time, but how is acceleration calculated? Sir Isaac Newton defined the following formula in 1687. It is known as **Newton's Second Law of Motion**.

\[
\text{Acceleration} = \left( \sum \text{Forces} \right) / \text{Mass}
\]

One definition of mass is a measure of an object's resistance to acceleration. The standard unit for mass is the kilogram (kg). **The mass of an object is calculated as the density times the area.** The standard unit for force is the newton [N = kg m/s\(^2\)], which is a vector quantity that represents mass times acceleration. Notice that dividing force by mass (kg) yields m/s\(^2\), which is acceleration. Distance is measured in meters.

Following the step-wise refinement principle, we explore the features of Box2D physics through a series of small examples. Since this is a book for beginners, we have implemented a "b2" class to facilitate physics coding. The easiest way to get started is to "fork" an existing Fiddle. The URLs that I used for development are listed next. The two JavaScript files can also be downloaded to run local tests via index.html, which enables easier use of the JavaScript debugger.
B2 and Box2d Library Links
https://raw.githubusercontent.com/bobcgausa/cook-js/master/b2.js
https://raw.githubusercontent.com/bobcgausa/cook-js/master/box2d-html5.js

I started work on the B2 library to provide a simple, and understandable, interface to Box2d, which has had the same API since its creation. I never imagined that I would end up with a 20K file comprised of 600 lines of code. There are many tutorials on JavaScript Box2D. If you wish, examine those for comparison.

The first step in creating a Box2D program is to choose a scale factor from pixels to meters. All of the examples in the tutorial use a scale of 30. Normally, all further dimensions would need to be expressed in fractions of meters. The B2 library only uses pixels as a unit and converts pixels to meters, and vice versa, automatically. In B2, the width of boxes and circles is always the diameter.

Box2D worlds are populated with bodies. Bodies can be composed from many shapes, referred to as fixtures in Box2D. The shapes in a body can accessed by index, 0, 1, etc. A body can be static, which means that it is frozen in place and cannot be moved by forces. The more common choice is to create dynamic bodies, which are affected by gravity and other forces. B2 will automatically delete bodies that fly off the left/right side of the screen and bodies that fall through the floor. Bodies that rise above the top of the screen are allowed to fall back into view.

Boxes and Circles

The first example creates a static floor and then drops a dynamic box from the top of the screen. Notice that the box and floor have a red outline, which is drawn because "debug drawing" was enabled by passing "true" to b2Draw. The b2Draw routine only draws the shapes that are associated with a body. For debugging, it can be useful to view joint connections, which are drawn when the debug argument is true.

Also notice that the default colors are a not-very-exciting, gray. B2 extends the properties that are defined in Box2D with additional, hopefully useful, properties, such as "display", which supports user-draw code.

Static Floor, Dynamic Dropped Box
http://jsfiddle.net/bobcook/fawk0u7b/

```javascript
function setup() {
  createCanvas(400, 300);
  b2newWorld(30, createVector(0, 9.8)); // scale and gravity
  // body type, dynamic/static, xy in pixels, wh in pixels
  new b2Body('box', false, createVector(width / 2, height - 2), createVector(width, 5)); // floor
  new b2Body('box', true, createVector(width / 2, 0), createVector(20,10)); // dropped box
}

function draw() {
```
background(227);
b2Update(); // **MUST** be present to update forces/position in Box2D
b2Draw(true); // default draw code for bodies, true/false controls debug drawing

The second example illustrates user-draw code and introduces the circle shape. Circles work well for balls, rocks, and other objects that can be treated as perfectly round when calculating collisions. If the visible sprite is round but irregular (say, a boulder or an egg), you may wish to set the radius slightly smaller than the physical image size.

To add a little excitement, clicking the mouse will randomly create a new box (red), circle (blue) or ellipse (green). The user has the choice between totally drawing a shape or simply setting the properties and then calling b2Display, which uses the matching P5 function to complete the figure. Observe that even though we are drawing an ellipse, the easiest approximation to its shape is a box. The most accurate approximation would be a polygon.

Some properties, such as "xy" or "static", are defined for bodies. Since a body can be composed of many shapes, the properties, such as "display", "type" or "wh", of individual shapes must be accessed by calling a function with the shape-index as an argument. A body that is composed of only one shape has an index of 0.

Observe that shapes on any body can share draw routines or each shape can be "display"ed with different functions.

**User-Draw Box/Circle/Ellipse Bodies**
http://jsfiddle.net/bobcook/q247oj9m/
function setup() {
    createCanvas(400, 300);
    b2newWorld(30, createVector(0, 9.8));
    var body = new b2Body('box', false, createVector(width / 2, height - 2), createVector(width, 5));
    body.display(attr, 0);
}

function draw() {
    background(227);
    b2Update();
    b2Draw(false); //no debugging
}

function mousePressed() {
    var body;
    if (random() < 0.3) {
        body = new b2Body('box', true, createVector(width / 2, 0), createVector(20,10));
        body.display(attr, 0); //shape index 0
    } else if (random() < 0.6) {
        //w is the circle's diameter
        body=new b2Body('circle', true, createVector(width / 2, 0), createVector(20,10));
        body.display(attr, 0);
    } else {
        body=new b2Body('box', true, createVector(width / 2, 0), createVector(20,10));
        body.display(attr1, 0);
    }
}

function attr(body, fixture, position) { --only set attributes
if (body.type(0) == 'box') fill(255,0,0);
else fill(0,0,255);
b2Display(body, fixture, position);
}

function attr1(body, fixture, position) { --take total control
    fill(0,255,0);
    ellipse(position.x, position.y, body.wh(0).x, body.wh(0).y);
}

## Edges and Polygons

The third example introduces edge and convex polygon shapes. Observe that the first two examples coded the floor as a static box. That choice gets unwieldy for bumpy surfaces. Remember that shapes are positioned at the center so trying to align the top corners to get an unbroken surface is a trial.

The static edge-shape solves the surface issue by connecting a list of lines to specify the boundaries of a world. The example defines a bumpy floor. Edge shapes are not restricted to 8 vertices and can contain concave dips. The vertices for both polygon and edge shapes are relative to the xy position of the body.

Click the mouse to drop circle or polygon shapes. The restitution of the circles is set high to illustrate different bounce values. Polygons are also specified as a list of lines; however, the last point is automatically connected to the first point. Polygon shapes can be created as static or dynamic bodies. Note that the **polygon coordinates must also be defined in counter-clockwise order**, and the resulting shape must be convex-only.

The optional arguments to the "b2Body" method are the first shape's density, friction, bounciness, and angle, which is the orientation in radians relative to its center.

- **density** is multiplied by the area of a body’s shape to determine its mass. This parameter is based on a standard value of 1.0 for water, so materials that are lighter than water (such as wood) have a density below 1.0, and heavier materials (such as stone) have a density greater than 1.0. The default value is 1.0.
- **friction** may be any non-negative value; a value of 0 means no friction and 1.0 means fairly strong friction. The default value is 0.5.
- **bounce** is the Box2d property known internally as “restitution”. It determines how much of an object’s velocity is conserved after a collision. Values greater than 0.3 are fairly “bouncy”. An object with a bounce value of 1.0 will rebound forever (i.e., if dropped to the ground, it will bounce back up to the height from which it was dropped). Bounce values higher than 1.0 are valid, but will cause strange behavior: objects will literally gain velocity with each collision until they fly off into space. The default value is 0.2, which is slightly bouncy.
- **angle** is the rotation of the box shape relative to its center. The default value is 0.0. Box2D only supports the rotation of boxes and polygons or edges.
function setup() {
    createCanvas(400, 300);
    b2newWorld(30, createVector(0, 9.8));
    new b2Body('edge', false, v(width / 2, height - 2),
                [v(-width/2, 0), v(-width/3,-20), v(0,0), v(width/3,-50), v(width/2,0)]);
}

function draw() {
    background(227);
    b2Update();
    b2Draw(true);
}

function mousePressed() {
    var body;
    if (random() < 0.5) {
        //density, friction, bounce
        body=new b2Body('circle', true, v(width / 2, 0), v(20,10), 1, 0.5, 0.6);
    } else {
        body=new b2Body('polygon', true, v(width / 2, 0), [v(15,-15), v(-25,0), v(-15,10), v(15,10)]);
    }
}

function v(x, y) {
    return createVector(x, y);
}

b2Body Methods and Properties
<table>
<thead>
<tr>
<th>Methods</th>
<th>Descriptions</th>
</tr>
</thead>
<tbody>
<tr>
<td><code>b2Body</code></td>
<td>type 'box' 'circle' 'polygon' 'edge'&lt;br&gt;xy is a P5 vector in pixels&lt;br&gt;wh is a P5 vector or an array of vectors (edge,polygon)</td>
</tr>
<tr>
<td><code>b2Body</code></td>
<td>angle is the rotation in radians and only affects the box shape.</td>
</tr>
<tr>
<td><code>b2Display</code></td>
<td>helper function for user-draw code. Just set the attributes, such as fill color, then call to draw. Supports the image property scaled to wh, except for polygons. The user can store additional properties in bodies and shapes.</td>
</tr>
<tr>
<td><code>b2GetBodyAt</code></td>
<td>returns null or the dynamic body that is located at pixel-position x/y. Used for mouse or finger-tap selection</td>
</tr>
<tr>
<td><code>body.toString()</code></td>
<td>returns x/y velocity.x/y, both in pixels.</td>
</tr>
<tr>
<td><code>body.destroy()</code></td>
<td>removes the body and all attachments from the world. Bodies are automatically destroyed if their &quot;life property is zero or if their position moves off the left, right, or bottom of the screen.</td>
</tr>
<tr>
<td><code>body addTo(type, xy, wh, angle)</code></td>
<td>add additional shapes to a body. The angle argument is optional. xy is the offset from the parent's center.</td>
</tr>
<tr>
<td><code>body.type(index)</code></td>
<td>index is optional in all these functions. If omitted, zero is assumed as the shape number. Returns one of 'box' 'circle' 'polygon' 'edge'</td>
</tr>
<tr>
<td><code>body.destroyShape(index)</code></td>
<td>removes the shape from the body/world, has no effect on other indices.</td>
</tr>
<tr>
<td><code>body.image(img, index)</code></td>
<td>sets the image property of a shape to a P5 image.</td>
</tr>
<tr>
<td><code>body.wh(index)</code></td>
<td>returns the wh value set in b2Body.</td>
</tr>
<tr>
<td><code>body.display(func, index)</code></td>
<td>sets the user-draw function for a shape. Set to null to restore the default.</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Properties</th>
<th>Descriptions</th>
</tr>
</thead>
<tbody>
<tr>
<td><code>body.static</code></td>
<td>returns true for a static body, false for dynamic.</td>
</tr>
<tr>
<td><code>body.active</code></td>
<td>returns true if the body is alive, false if deletion is pending.</td>
</tr>
<tr>
<td><code>body.visible</code></td>
<td>get or set to true/false to control drawing.</td>
</tr>
<tr>
<td><code>body.life</code></td>
<td>get or set to number of time steps until destruction, default 10000000.</td>
</tr>
<tr>
<td><code>body.density</code></td>
<td>get or set density on all attached shapes.</td>
</tr>
<tr>
<td><code>body.friction</code></td>
<td>get or set friction on all attached shapes.</td>
</tr>
<tr>
<td>Method</td>
<td>Description</td>
</tr>
<tr>
<td>-----------------</td>
<td>--------------------------------------------------</td>
</tr>
<tr>
<td>body.bounce</td>
<td>get or set restitution on all attached shapes.</td>
</tr>
<tr>
<td>body.xy</td>
<td>returns a P5 vector for the current position in pixels.</td>
</tr>
<tr>
<td>body.angle</td>
<td>returns the rotation of a body in radians.</td>
</tr>
<tr>
<td>body.mass</td>
<td>returns the weight in kilograms.</td>
</tr>
<tr>
<td>body.centerOfMass</td>
<td>returns a P5 vector for the mass center of a body in pixels.</td>
</tr>
<tr>
<td>body.classOf</td>
<td>returns 'b2Body'.</td>
</tr>
</tbody>
</table>

**Multi-Shape Bodies**

Using rectangles and circles as game objects is not very interesting. Players expect exciting images. The physics coders task is to partition images into convex polygons of no more than 8 vertices each. There are a number of applications, such as the Physics Editor (www.codeandweb.com/physicseditor), to automate the conversion. The shapes are used in the physics model, but the program displays the images.

In the next example, we define a body composed of a circle, a box, and a polygon. Remember that add-ons use coordinates to the host body's xy position. Further, each add-on also has an xy origin. This feature is useful for polygons as it allows shape definitions to be repositioned on the same, or different figures.

The "addTo" function adds shapes to a body. The arguments are an parent-offset xy-position, the width and height or an array of coordinates, and an optional angle, which only applies to boxes (as illustrated). The "display" property is set to a user-draw function to override the default fill color. Box2D does not require that a body's shapes touch each other. The shapes can have empty space between them, but the components always retain their defined orientation with a body's position. Observe that the box shape has been rotated relative to the body.

**Multi-Shape Example**

http://jsfiddle.net/bobcook/4rd29f09/
function setup() {
    createCanvas(400, 300);
    b2newWorld(30, createVector(0, 9.8));
    new b2Body('edge', false, v(width / 2, height - 2),
                [v(-width/2, 0), v(-width/3,-20), v(0,0), v(width/3,-50), v(width/2,0)]);
}

function draw() {
    background(227);
    b2Update();
    b2Draw(true);
}

function mousePressed() {
    var body = new b2Body('circle', true, v(width / 2, 0), v(20,10));
    body.display(foo);
    body.addTo('polygon', v(0, -20), [v(15,-15), v(-25,0), v(-15,10), v(15,10)]);
    body.display(foo, 1);
    body.addTo('box', v(20, 0), v(15, 15), PI/3);
    body.display(foo, 2);
}

function foo(body, fixture, position) {
    fill(0, 255, 0);
    b2Display(body, fixture, position);
}

function v(x, y) {
    return createVector(x, y);
}
Body Selection

The final body example illustrates how to convert mouse coordinates to a body reference. The first time that a body is touched, its color will change to blue. The second touch on the same body will delete it. There are many game applications for mouse selection. Observe that the code adds the user-defined "touched" property to each body.

Body Selection Example
http://jsfiddle.net/bobcook/te2eo0q0/

```
//only the changed code
function mousePressed() {
    var b = b2GetBodyAt(mouseX, mouseY);
    if (b != null) {
        if (b.touched++ > 0) b.destroy();
        return;
    }
    // same as before
}

function foo(body, fixture, position) {
    fill(0, 255, body.touched!=0 ? 255 : 0);
    b2Display(body, fixture, position);
}
```

Applying Force

In the previous examples, gravity was the primary force, although body collisions also imparted forces. In order to model the physics of projectiles, the shooting-throwing-slinging mechanism must be able to apply a force at one or more points on a body. Similarly, driving a car requires that forces be applied to the chassis.
The default point in Box2D at which force is applied is the **center of mass**. For rigid bodies, the center of mass is the centroid. Remember that in Box2D the mass of a body equals the density times its area. Informally, the **centroid** is the point at which a cardboard cut-out of a body could be perfectly balanced on the tip of a pencil. The centroid is important because a force applied at that point moves an object in the direction of the force. Pushing a toy block at an edge will rotate it. Pushing a toy block in the center of a side will slide it backwards.

![Center of Mass](image)

The Box2d body API defines a number of properties and methods to apply and regulate forces. The first example only uses one of the methods "applyForce". The object:applyForce() method adds (vector-wise) the specified x and y components of a force at a given point in or on an object. If the target point is the body's center of mass, it will tend to push the body in a straight line. If the target point is offset from the center, the body will spin around its center of mass. For symmetrical objects, the center of mass and the center of the object will have the same position. The force is not applied immediately but rather is factored into the physics engine's next time step and combined with other forces, such as gravity. Just as a car glides to a halt if its motor is turned off, a force that is just applied once will not keep a body moving for long.

Think of the "xyForce" vector as the steering wheel of a car that is omni-directional and the "power" value as the gas pedal.

```javascript
body.applyForce( xyForce, power )
```

In the cannon example, we stack cans then the player shoots cannon balls to try to knock them all off the wall. The following code draws the scene and stacks the cans. When the mouse is pressed, a circular cannon ball is created and fired in the direction of the mouse click. The ball is set to a higher density than the cans, which would be the case in real life.

**Cannon Ball Shooter**

http://jsfiddle.net/bobcook/8djgkc24/
function setup() {
  createCanvas(400, 300);
  b2newWorld(30, createVector(0, 9.8));
  base(width / 2, height - 2, width, 5);
  pyramid(5, width*3/4, height - 10, 16, 32);
}

function draw() {
  background(227);
  b2Update();
  b2Draw(true);
}

function mousePressed() {
  var b = shape('circle', 5, height - 8, 20, 20);
  b.density = 20;
  b.applyForce(createVector(1, (height - mouseY)/height*2), 300);
}

function base(x, y, w, h) {
  return new b2Body('box', false, createVector(x, y), createVector(w, h));
}

function shape(type, x, y, w, h) {
  return new b2Body(type, true, createVector(x || width / 2, y || 0), createVector(w || 20, h || 20));
}
```javascript
function pyramid(n, x, y, w, h) {
    // Build a pyramid with an n-can base
    var xy = createVector(x,y);
    var wh = createVector(w,h);
    while (n > 0) {
        var i = 0;
        var _xy = xy.copy();
        while (i < n) {
            var b = shape('box', _xy.x, _xy.y, wh.x, wh.y);
            b.density = 5;
            _xy.x += wh.x / 2 + wh.x;
            i++;
        }
        n--;
        xy.x += wh/2+wh.x/4;
        xy.y -= wh.y*3/2;
    }
}
```

Shooting an object is easy. Just touch the screen and a new ball is created at the y-coordinate height, and then thrown with a power of 300. The code could easily be turned into a game by gradually increasing the number and types of cans. Remember that off-screen balls and cans are deleted automatically.

The following table lists the properties and methods for a Box2D body. Forces are specified either in pixels for straight-line application or in radians for rotation. Remember that the P5 radians() function will convert degrees to radians.

<table>
<thead>
<tr>
<th>Body Force Methods and Properties</th>
<th>Methods</th>
<th>Descriptions</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>body.applyForce(xyForce, nPower)</td>
<td>Applies the vector force (multiplied by nPower) in pixels/second over multiple time steps at the center of mass taking into account other forces, such as gravity.</td>
</tr>
<tr>
<td></td>
<td>body.applyImpulse(xyForce, nPower)</td>
<td>Adds in the vector force (multiplied by nPower) in pixels/second immediately. If there are, for example, 30 time steps per second, this means the effect will be magnified by a factor of 30 over applyForce.</td>
</tr>
<tr>
<td></td>
<td>body.applyTorque(radians)</td>
<td>Applies a rotational force to the body over multiple time steps. Positive values will result in clockwise rotation; negative values will result in counter-clockwise torque. The body will rotate about its center of mass.</td>
</tr>
</tbody>
</table>
body.applyAngularImpulse(radians) | Adds a rotational force immediately.
---|---
body.sensor(bool, index) | Turns the sensor property of a shape on (true) or off (false).
body.isSensor(index) | Returns the sensor property of a shape.

<table>
<thead>
<tr>
<th>Properties</th>
<th>Descriptions</th>
</tr>
</thead>
<tbody>
<tr>
<td>body.gravityScale</td>
<td>Sets the effect of gravity on the body. Setting it to 0 makes the body float, even if other objects in the simulation are subject to normal gravity. The default value is 1.0 (normal gravity).</td>
</tr>
<tr>
<td>body.bullet</td>
<td>Get or set to true/false. Prevents fast-moving objects from passing through thin barriers.</td>
</tr>
<tr>
<td>body.velocity</td>
<td>Returns the xy-velocity in pixels per second.</td>
</tr>
<tr>
<td>body.collision</td>
<td>Gets or sets the collision listener function, func(body1, body2).</td>
</tr>
<tr>
<td>body.categories</td>
<td>A category defines which bodies collide. The default category is 1. A category of 0 does not collide. Other category selectors are 2, 4, 8, 16, 32, 64, 128, 256, 512, 1024, 2048, 4096, 8192, 16384, 32768. A body can be a member of multiple categories e.g. 256+8+1.</td>
</tr>
<tr>
<td>body.collidesWith</td>
<td>Lists the categories with which this body collides. Colliding with all categories is the default. Zero indicates no collisions. Specify as 2048+32+1 for readability.</td>
</tr>
</tbody>
</table>

The "bullet" property is set on any body that moves "fast" relative to the obstacles that it might encounter. Basically, if the velocity step in pixels is larger than the width of an obstacle, collisions might not be detected. The game programming term is **tunneling**. Try running the following sample code with, and without, the bullet property set. Observe that that it takes a much lower "impulse" to shoot the bullet. Try switching between Force and Impulse.

**Tunneling Example**
http://jsfiddle.net/bobcook/cy8rr9ep/
```javascript
function setup() {
    createCanvas(400, 300);
    b2newWorld(30, createVector(0, 9.8));
    base(width / 2, height - 2, width, 5);
    // Stacked Boxes
    for (var i = 0; i < height / 2 / 25; ++i) {
        var b = shape('box', width * 2 / 3, height - 5 - i * 10 - 20, 5, 10);
    }
}

function draw() {
    background(227);
    b2Update();
    b2Draw(true);
}

function mousePressed() {
    var b = shape('circle', 20, height - 8, 3, 3);
    b.bullet = true; //collision not detected without the flag
    b.applyImpulse(createVector(1, 0), 0.4);
}

function base(x, y, w, h) {
    return new b2Body('box', false, createVector(x, y), createVector(w, h));
}

function shape(type, x, y, w, h) {
    return new b2Body(type, true, createVector(x || width / 2, y || 0), createVector(w || 20, h || 20));
}

Torque Example
http://jsfiddle.net/bobcook/8djgkc24/
```
```javascript
function mousePressed() {
    var b = shape('box', 5, height-80, 40, 10);
    b.density = 20;
    b.gravityScale = 0; //unaffected by gravity
    b.applyForce(createVector(1, (height-mouseY)/height*2), 300);
    b.applyTorque(550.0); //positive is clockwise
}
```

**Collisions**

A typical game implements bodies that collide, such as characters and swords, as well as bodies that should not collide, such as the particles in an explosion or a rider on a bicycle. By default, all objects, both static and dynamic, collide with each other.

The library defines a "collision" property on bodies that can be set to a collision-listener function. Each body can attach its own listener, or bodies can share a function.

In the next example, circles are dropped at random X locations. When a collision is detected between two bodies, the listener is invoked. The color on one body is set to green and the color of the other body is set to cyan. Running the example illustrates that the color of a colliding body can oscillate between cyan and green; in other words, there is no fixed order in which body is number one or two.

**Collision Listener Function**

http://jsfiddle.net/bobcook/ajewna8r/
function setup() {
    createCanvas(400, 300);
    b2newWorld(30, createVector(0, 9.8));
    new b2Body('edge', false, v(width / 2, height - 2), [v(-width/2, 0), v(width/2,0)]);
}

function draw() {
    background(227);
    var b = new b2Body('circle', true, v(random(12,width-12),12), v(20,20));
    b.color = color(255,0,0);
    b.display(drawer);
    b.collision = bump;
    b2Update();
    b2Draw(false);
}

function drawer(body, shape, position) {
    fill(body.color);
    ellipse(position.x, position.y, 20, 20);
}

function bump(body1, body2) {
    body1.color = color(0,255,0);
    body2.color = color(0,255,255);
}

function v(x, y) {
    return createVector(x, y);
}
It is a common practice in programming to add redundant features because they provide a performance advantage. Such is the case with collision categories.

The programmer could resolve all collision tests in the "bump" function as listed in the previous example. However, it is more efficient to let the Box2D library "filter" unwanted collisions before they are propagated to the user.

Box2D provides 16 collision categories (1, 2, ..., 32768). Any body can be a member of any, all, or none of the categories. It is recommended to list the categories as a sum, such as 8+2+1. The default category is one for both static and dynamic bodies.

The "collidesWith" property of a body specifies the list of categories with which it collides. Again, it is recommended to list the categories as a sum from high to low.

### Box2D Collision Formula

IF \( \text{body1.categories matchesOneOf body2.collidesWith} \) OR \( \text{body2.categories matchesOneOf body1.collidesWith} \) THEN CALL_USER_CODE

<table>
<thead>
<tr>
<th>Categories</th>
<th>CollidesWith</th>
<th>Result</th>
</tr>
</thead>
<tbody>
<tr>
<td>body1 = 4</td>
<td>4</td>
<td>only collides with other 4s</td>
</tr>
<tr>
<td>body1 = 4</td>
<td>8</td>
<td>collides with 8s but not 4s</td>
</tr>
<tr>
<td>body1 = 4</td>
<td>8+4</td>
<td>collides with 8s and 4s</td>
</tr>
</tbody>
</table>

If two bodies touch but do not "collide", Box2D will allow the shapes to pass through each other or to overlap with no bounce or force calculation. Collision can also be asymmetric; that is, body1 can collide with the category of body2 without requiring that body2 also specify a collision.

The next example creates both boxes (category 2) and circles (category 4). Both shapes collide with themselves and the ground (remember default of 1), but not each other. Observe that both shapes form overlapping pyramids. As in the previous example, red shapes change color to green or cyan upon a collision.

### Collision Categories

http://jsfiddle.net/bobcook/0tdnomtk/
function setup() {
  createCanvas(400, 300);
  b2newWorld(30, createVector(0, 9.8));
  new b2Body('edge', false, v(width / 2, height - 2), [v(-width/2, 0), v(width/2,0)]);
}

function draw() {
  background(227);
  var b;
  if (random() < 0.5) {
    b = new b2Body('circle', true, v(random(12,width-12),12), v(20,20));
    b.categories = 4;
    b.collidesWith = 4+1;
  } else {
    b = new b2Body('box', true, v(random(12,width-12),12), v(20,10));
    b.categories = 2;
    b.collidesWith = 2+1;
  }
  b.color = color(255,0,0);
  b.display(drawer);
  b.collision = bump;
  b2Update();
  b2Draw(false);
}

function drawer(body, shape, position) {
  fill(body.color);
  if (body.type()=='circle') ellipse(position.x, position.y, 20, 20);
  else rect(position.x, position.y, 20, 10);
}
function bump(body1, body2) {
  var col;
  if (body1.type() == 'circle') col = color(0,255,0);
  else col = color(0,255,255);
  body1.color = col; body2.color = col;
}

function v(x, y) {
  return createVector(x, y);
}

Sensors

Sensors are a great feature of Box2D. A sensor calls a collision listener when a collision occurs; however, the physical effects of the collision are not applied. For example, consider a car's headlights. They illuminate obstacles in front of a car, but the light does not trigger a physical collision. In addition to headlights, sensors can be used for airplane radar, bug feelers, game proximity triggers, and many other applications.

In the sensor example, boxes and circles are dropped from the top of the screen. As the shapes pass through the colored sensor circles, the collision listener assigns a new color.

Sensor Example
http://jsfiddle.net/bobcook/ov5n9pqt/
function setup() {
    createCanvas(400, 500);
    b2newWorld(30, createVector(0, 9.8));
    new b2Body('edge', false, v(width / 2, height - 2), [v(-width/2, 0), v(width/2,0)]);
    create(6, color(255,0,0));
    create(3, color(0,255,0));
    create(2, color(0,0,255));
    create(1.5, color(255,0,255));
    create(1.1, color(0,255,255));
}

function create(fraction, col) {
    var b = new b2Body('circle', false, v(width / fraction, height/2), v(40, 40));
    b.display(drawer);
    b.color = col;
    b.sensor(true);
    b.categories = 2;
    b.collidesWith = 2;
    b.collision = bump;
}
```javascript
function draw() {
    background(227);
    var b;
    if (random() < 0.5) {
        b = new b2Body('circle', true, v(random(12,width-12),12), v(20,20));
    } else {
        b = new b2Body('box', true, v(random(12,width-12),12), v(20,10));
    }
    b.categories = 2;
    b.collidesWith = 2+1;
    b.color = color(200, 200, 200);
    b.display(drawer);
    b2Update();
    b2Draw(false);
}

function drawer(body, shape, position) {
    fill(body.color);
    if (body.type()=='circle') ellipse(position.x, position.y, body.wh().x, body.wh().x);
    else rect(position.x, position.y, 20, 10);
}

function bump(body1, body2) {
    var col;
    if (body1.isSensor()) body2.color = body1.color; //transfer color
    else body1.color = body2.color;
}

function v(x, y) {
    return createVector(x, y);
}

Joints

The human body has joints everywhere. Bones are rigid bodies that are acted on by internal forces applied by muscles and by external forces, such as gravity, and those applied by the environment. There are many different kinds of human joints.

Box2D implements a number of different joints. We only discuss some of the options. The examples are constructed with the goal of providing cut-and-paste code that the reader can use to model common game physics. All Box2D joints are created with the "b2Joint" method.

<table>
<thead>
<tr>
<th>Joint Creation and Methods</th>
</tr>
</thead>
<tbody>
<tr>
<td>b2Joint(typeName, bodyA, bodyB, properties)</td>
</tr>
<tr>
<td><strong>Properties</strong></td>
</tr>
<tr>
<td>(name: value, adds a joint to bodyA. A body can have multiple joints, which are</td>
</tr>
<tr>
<td>Function</td>
</tr>
<tr>
<td>----------</td>
</tr>
<tr>
<td><code>typeName</code></td>
</tr>
<tr>
<td><code>distance</code>, <code>rope</code></td>
</tr>
<tr>
<td><code>distance</code>, <code>mouse</code>, <code>wheel</code></td>
</tr>
<tr>
<td><code>distance</code>, <code>mouse</code>, <code>wheel</code></td>
</tr>
<tr>
<td><code>distance</code>, <code>mouse</code>, <code>pulley</code>, <code>revolute</code>, <code>rope</code>, <code>wheel</code></td>
</tr>
<tr>
<td><code>mouse</code>, <code>wheel</code></td>
</tr>
<tr>
<td><code>revolute</code>, <code>wheel</code></td>
</tr>
<tr>
<td><code>revolute</code>, <code>wheel</code></td>
</tr>
<tr>
<td><code>revolute</code>, <code>wheel</code></td>
</tr>
<tr>
<td><code>pulley</code></td>
</tr>
<tr>
<td><code>pulley</code></td>
</tr>
<tr>
<td><code>pulley</code></td>
</tr>
<tr>
<td><code>pulley</code></td>
</tr>
<tr>
<td><code>body.destroyJoint(index)</code></td>
</tr>
<tr>
<td><code>body.motorOn(true/false, index)</code></td>
</tr>
<tr>
<td><code>body.isMotorOn(index)</code></td>
</tr>
<tr>
<td><code>body.motorSpeed(newValue, index)</code></td>
</tr>
<tr>
<td><code>body.getMotorSpeed(index)</code></td>
</tr>
<tr>
<td><code>body.maxMotorTorque(newValue, index)</code></td>
</tr>
<tr>
<td><code>body.getMaxMotorTorque(index)</code></td>
</tr>
</tbody>
</table>
Mouse Joint

A mouse joint creates an elastic connection between an object and your mouse/finger, which makes the object attempt to follow the drag-path. But since the object remains under simulation, its motion may be stopped by other bodies in the world. Also, an object will rotate realistically under gravity when "picked up by one end".

The action of this joint is not automatic. The location of its attached body must be updated by calling setTarget(xy). The method can be called from a mouse/touch routine.

The overall speed or "lag" of the joint depends on the force exerted, which is stored in the maxForce property. By default, the attribute is set to 1000 times the mass of the body, which allows for fairly rapid dragging.

In the example, the selected shape follows the mouse, or touch, motion until the contact is released. When the mouse button is released, the shape drops to the ground.

Mouse Joint Example
http://jsfiddle.net/bobcook/fpcy09a0/

```javascript
var mouse = null;

function setup() {
  createCanvas(400, 300);
  b2newWorld(30, createVector(0, 9.8));
  new b2Body('box', false, v(width / 2, height - 2), v(width, 5));
}
```
function draw() {
    background(200, 200, 200);
    b2Update();
    if (mouse != null) mouse.setTarget(v(mouseX, mouseY));
    b2Draw(true);
}

function keyTyped() {
    var t;
    if (key == 'b') {
        t = new b2Body('box', true, v(width / 2 - 2, 0), v(50, 20));
        t.addTo('box', v(0, -70 / 2 - 20 / 2), v(50, 50), PI / 4);
        t.display(foo, 1);
        t.applyAngularImpulse(10);
    } else if (key == 'c') {
        t = new b2Body('circle', true, v(width / 2, 0), v(50, 50));
    }
    t.display(foo);
}

var foo = function (body, fixture, pos) {
    fill(255, 0, 0);
    stroke(0, 255, 0);
    strokeWeight(2);
    b2Display(body, fixture, pos);
}

function mousePressed() {
    var b = b2GetBodyAt(mouseX, mouseY);
    if (b == null) return;
    mouse = b;
    b2Joint("mouse", null, b, {
        xy: v(mouseX, mouseY)
    });
}

function mouseReleased() {
    if (mouse != null) mouse.destroyJoint();
    mouse = null;
}

function v(x, y) {
    return createVector(x, y);
}

Revolute Joint
A revolute, or pivot, joint can model a hinge, a pin, or an axle that connects one body to another. The point of connection must be specified. It would not make sense to connect two static objects with a pivot joint, but any other combination has uses. The body can swing freely around the pivot point.

The really exciting feature of revolute joints is that they can have built-in motors. As a result, the motors can power body parts, flippers or any other mechanized device. Revolute joints can also be linked to create flexible structures such as chains or bridges.

By default, the motors have a fairly weak maximum torque, thus setting motorSpeed may appear to have little visible effect. Therefore, you should generally set maxMotorTorque to a high value (such as 10000) if you are trying to move any significant mass.

The following example updates the colored sensor example to create five colored, rotating flippers. When the falling shapes touch a flipper, the color changes. Shapes can be flipped into the air from one sensor to another before falling to the ground. Try un-commenting the sensor property, which will cause shapes to pass through but still change color if touched. Try changing the motor speed and torque values. Observe that if a motor is disabled, the flipper will still spin, but only in reaction to collision forces.

**Revolute Joint Example**

http://jsfiddle.net/bobcook/750q8oz8/
//ONLY CODE THAT CHANGED FROM SENSOR EXAMPLE

function create(fraction, col) {
    var b = new b2Body('box', true, v(width / fraction, height/2), v(60, 10));
    b.display(drawer);
    b.color = col;
    //b.sensor(true);
    b.categories = 2;
    b.collidesWith = 2;
    b.collision = bump;
    b.bumper = true;
    var c = new b2Body('circle',false,v(width/fraction,height/2),v(10,10));
    c.categories = 0;
    c.collidesWith = 0;
    b2Joint("revolute",c,b,{speed: PI*2, maxTorque:10000, enable:true});
}

function drawer(body, shape, position) {
    fill(body.color);
    b2Display(body, shape, position);
}
function bump(body1, body2) {
  if (body1.bumper) body2.color = body1.color;
  else body1.color = body2.color;
}

Wheel Joint

A wheel joint can model a wheel that is connected to a body by a shock absorber. The point of connection must be specified as an offset that is relative to the center of the vehicle. As with a revolute joint, a motor can be enabled to drive a vehicle forwards, or backwards. Since Box2D simulates a 2D world, typically only two wheels are attached.

The following car example attaches two wheel joints (with motors) to a vehicle. Typing 'd' or 'a' will drive the vehicle forwards or backwards, respectively.

Wheel Joint Example
http://jsfiddle.net/bobcook/k9d7tohn/

var hz = 4;
var zeta = 0.7;
var speed = 0;
var car;

function setup() {
  createCanvas(600, 300);
  b2newWorld(30, v(0, 9.8));
  var ground = new b2Body('edge', false, v(0, height - 20), [v(0, -height), v(0, 0), v(200, 0), v(300, -20), v(400, -10), v(600, 0), v(600, -height)));
  car = new b2Body('polygon', true, v(50, height - 55), [v(-30, 10), v(30, 10), v(30, 0), v(0, -18), v(-23, -18), v(-30, -4)));
  var wheel1 = shape('circle', 30, height - 35, 16); //back
  wheel1.friction = 0.9;
  var wheel2 = shape('circle', 70, height - 35, 16); //front
  wheel2.friction = 0.9;
  b2Joint('wheel', car, wheel2, {
Rope, Distance, and Pulley Joints

The three joints discussed in this Section are the rope, distance, and pulley joints. Again, each joint connects two objects; however, the objects are not overlapping, but are separated at a distance.
The Rope joint connects two objects with an invisible rope that connects the two center points. The distance between the centers is the length of the rope. The connection is not elastic so it can be shrunk, but is very resistant to stretching.

```javascript
var rope1 = b2Joint("rope", point, circle, {separation: 140} )
```

The Distance joint is basically a Rope joint with lots of tuning parameters. The default length of the invisible rope is the distance between the two anchor points. However, a length property is defined for Distance joints so that the length can be set shorter or longer than the original distance. If one of the body types is static, the other body will move from its initial location to one that has the right distance from the first body's anchor point.

```javascript
var dist = b2Joint("distance", point, circle, {separation: 80, frequency: 0.7, damping: 0.1} );
```

Another cool feature of Distance joints is that they can be springy; that is, the invisible rope can shorten and lengthen at a certain frequency like a weight on a rubber band. The two control properties are "frequency" and "damping".

"The distance joint can also be made soft, like a spring-damper connection. Softness is achieved by tuning two constants in the definition: frequency and damping ratio. Think of the frequency as the frequency of a harmonic oscillator (like a guitar string). The frequency is specified in Hertz. Typically the frequency should be less than half the frequency of the time step. So if you are using a 60Hz time step, the frequency of the distance joint should be less than 30Hz. The reason is related to the Nyquist frequency. The damping ratio is non-dimensional and is typically between 0 and 1, but can be larger. At 1, the damping is critical (all oscillations should vanish)." [from Box2D]

At a frequency of zero or a damping value of one, a distance joint acts like a rope. Otherwise, forces on the bodies will induce a bouncing effect. The first bounce may even "shoot" one of the objects past the other anchor point. The damping value governs how quickly the bouncing slows down. Higher values will slow objects faster.

Pulleys have been used for thousands of years to make it possible to lift heavy loads through force multiplication. By using the right pulley configuration, 50kg of weight can be lifted by applying 10kg of force. With Box2D, complicated block-and-tackle pulley structures are unnecessary; only the force ratio needs to be specified.

A Pulley joint attaches two bodies with an invisible rope that tries to keep its length constant: if one body is pulled down, the other one will move up. The b2Joint method is a bit complicated because it must specify two bodies and two stationary anchor points in world coordinates for each side of the rope to hang from.

```javascript
joint = b2Joint( "pulley", bodyA, bodyB, {
    xy: createVector(140, 160),
    xyb: createVector(190, 140),
```
lengthA: 30,  
lengthB: 40,  
ratio: 0.6
})

The ratio argument simulates a block and tackle arrangement in which one side of the rope moves faster than the other. By default, this ratio is 1.0, which models a simple pulley. Each body can swing and rotate on its end of the invisible rope if forces are applied. Note that trying to pull one of the bodies past its anchor point results in bizarre behavior.

The example, which is illustrated in the next Figure, implements an instance of each of these joint types. Further, each of the circles can be touch-dragged to view the effect of different forces on the joints. The Figure is drawn in "debug" mode to show the movements of the invisible ropes.

**Distance, Rope, Pulley Joint Example**  
http://jsfiddle.net/bobcook/81emgjnL/

```javascript
var mouse = null;
var mouseIndex;

function setup() {
  createCanvas(400, 300);
  b2newWorld(30, v(0, 9.8));
  new b2Body('box', false, v(width / 2, height - 2), v(width, 5));
  var b1 = base(250, 50);
  var b2 = circle(250, 80);
  b2Joint("distance", b1, b2, {
    separation: 80,
    frequency: 0.7,
    damping: 0.1
  });
  b1 = base(150, 50);
```
b2 = circle(150, 100);
b2Joint("rope", b1, b2, {
    separation: 140
});
b1 = circle(140, 180);
b2 = circle(190, 180);
b2Joint("pulley", b1, b2, {
    xy: v(140, 160),
    xyb: v(190, 140),
    lengthA: 30,
    lengthB: 40,
    ratio: 0.6
});
}

function draw() {
    background(227);
b2Update();
    if (mouse != null) mouse.setTarget(v(mouseX, mouseY), mouseIndex);
b2Draw(true);
}

function base(x, y) {
    return new b2Body('box', false, v(x, y), v(10, 10));
}

function circle(x, y) {
    return new b2Body('circle', true, v(x, y), v(20, 20));
}

function mousePressed() {
    var b = b2GetBodyAt(mouseX, mouseY);
    if (b == null) return;
    mouseIndex = b2Joint("mouse", null, b, {xy: v(mouseX, mouseY)});
    mouse = b;
}

function mouseReleased() {
    if (mouse != null) mouse.destroyJoint(mouseIndex);
    mouse = null;
}

function v(x, y) {
    return createVector(x, y);
}
Alien Attack

The Alien Attack game flies alien spacecraft from left to right on the screen. If a craft makes it through the defensive perimeter on the right side of the screen, the player loses 100 points. The player has an array of weapons on the right side of the screen. The weapons shoot projectiles toward locations as they are clicked/tapped by the player; however, each weapon has a fixed fire rate and reload time. If the player destroys a craft or knocks it off the screen, the player gains 100 points.

The example embodies the design principle that we love best (step-wise refinement). The program is fairly simple; however, it utilizes two sophisticated classes (Fountain and Projectile), which were built and tested in the order listed before the main code was ever written.

Fountains

The Fountain class was a refinement of the earlier Particle class. I started the implementation by passing the shape names to the class but that soon proved inflexible and unwieldy. It was an example of trying to do too many things in one piece of code. Every addition of a shape required the insertion of the corresponding drawing code in the class.
The better solution was to pass the name of the shape-drawing code as an argument. The name is then used as an index into a table of function values. Users can now add new shape names and attach drawing routines without touching the Fountain code.

Particles are defined as a table. One of the notable features of the design is that the view of a particle is totally separated from its actions. The Particle "life" property is defined as a fraction from 0 to 1. The fraction can then be used to select different display attributes, such as color, over a particle's lifetime. Particles have location and size properties as well as linear and angular velocities.

```javascript
function Particle() {
    this.xVel = 0;
    this.yVel = 0;
    this.partSize = 0;
    this.x = 0;
    this.y = 0;
    this.life = 0;
    this.rotation = 0;
}
```

Fountains can be defined in a JSON file or string. The JSON specifies an array of named fountain definitions. After the JSON is loaded, the converted object is passed as an argument to the Fountain class' constructor to create new fountains. The following table illustrates the JSON properties.

The Fountain definition is listed as a Fiddle that inputs a JSON Fountain string. Change the properties to become familiar with particle effects. To experiment with image-based particles, the example must be run on a PC or tablet. Particle generation is a sophisticated technical area. Our definition only includes the basics. See particle2dx.com for other options, which could be easily added.

<table>
<thead>
<tr>
<th>Name</th>
<th>Description</th>
<th>Example</th>
</tr>
</thead>
<tbody>
<tr>
<td>name</td>
<td>unique name for this fountain</td>
<td>&quot;name&quot;: &quot;foo&quot;</td>
</tr>
</tbody>
</table>
| color  | array of color names or [R,G,B,A] values. If more than one color is specified, the color changes in 1/length lifetime steps. Alpha | "color": ["orange",[255,0,0],"yellow","white","white","white"] }
<table>
<thead>
<tr>
<th>Parameter</th>
<th>Description</th>
<th>Example</th>
</tr>
</thead>
<tbody>
<tr>
<td>values</td>
<td>can be changed to fade particles in or out. Color should be white for images but other colors or alpha values can be listed as tints.</td>
<td>&quot;shape&quot;: &quot;rect&quot;</td>
</tr>
<tr>
<td>shape</td>
<td>string index into the fdisplay array to select a drawing function.</td>
<td>&quot;gravity&quot;: 0.1</td>
</tr>
<tr>
<td>gravity</td>
<td>added to yVelocity at each Step.</td>
<td>&quot;sizePercent&quot;: 0.999</td>
</tr>
<tr>
<td>sizePercent</td>
<td>particle size is multiplied by this value at each Step. Fractions less than one shrink a particle, greater than one expands a particle.</td>
<td>&quot;angle&quot;: [190,300]</td>
</tr>
<tr>
<td>angle</td>
<td>defines the spread of the particle stream in degrees.</td>
<td>&quot;speed&quot;: 5.5</td>
</tr>
<tr>
<td>speed</td>
<td>velocity is set by a random angle and multiplied by speed.</td>
<td>&quot;limit&quot;: 250</td>
</tr>
<tr>
<td>limit</td>
<td>number of particles generated at one particle per Step.</td>
<td>&quot;lifetime&quot;: 200</td>
</tr>
<tr>
<td>lifetime</td>
<td>number of Steps before the particle is deleted.</td>
<td>&quot;size&quot;: [4,12]</td>
</tr>
<tr>
<td>size</td>
<td>defines the range of particle sizes.</td>
<td>&quot;rotation&quot;: 2</td>
</tr>
<tr>
<td>rotation</td>
<td>angular velocity in degrees. If non-zero, the initial</td>
<td></td>
</tr>
</tbody>
</table>

**Optional**
rotation is random(0, 360).

<table>
<thead>
<tr>
<th>file</th>
<th>path to an image file. Images are scaled by partSize.</th>
<th>&quot;file&quot;: &quot;assets/fire.png&quot;</th>
</tr>
</thead>
<tbody>
<tr>
<td>x</td>
<td>sets particle x-origin to width/x.</td>
<td>&quot;x&quot;: 2</td>
</tr>
<tr>
<td>y</td>
<td>sets particle y-origin to height/y.</td>
<td>&quot;y&quot;: 2</td>
</tr>
<tr>
<td>edges</td>
<td>array of vectors that define counter-clockwise points (relative to xy) in a polygon</td>
<td>&quot;edges&quot;: [[5,-5],[-5,-5],[0,5]]</td>
</tr>
</tbody>
</table>

**JSON Examples**

```javascript
var defs;
var of, mf, sf;
function preload() {
    defs = loadJSON('assets/fountains2.txt');
}
function setup() {
```
createCanvas(320, 320);
of = new Fountain(defs, "foo");
mf = new Fountain(defs, "boo");
sf = new Fountain(defs, "soo");
}

function draw() {
    background(127);
of.Draw();
of.Create();
of.Step();
mf.Draw();
mf.Create();
mf.Step();
sf.Draw();
sf.Create();
sf.Step();
noStroke();
text(of.length, width - 60, 20);
stroke(0);
}
**new** Fountain(JSON table, name, x, y)  
xy are optional and specify the pixel origin for the fountain. If omitted, JSON xy are used.

Create(x, y)  
xy are optional and specify the pixel origin of this particle. Creates one particle unless the limit has been exceeded. Returns an instance of Particle.

Draw()  
draws all particles in this fountain.

Step()  
advances positions of all particles and deletes particles if their life is over.

Stop()  
stops the fountain and deletes all particles.

**Properties**

<table>
<thead>
<tr>
<th>Property</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>particles[]</td>
<td>array of active particles.</td>
</tr>
<tr>
<td>f</td>
<td>reference to the JSON table entry for this fountain.</td>
</tr>
<tr>
<td>colors[]</td>
<td>f.color array converted to P5 colors</td>
</tr>
<tr>
<td>x</td>
<td>pixel origin position</td>
</tr>
<tr>
<td>y</td>
<td>pixel origin position</td>
</tr>
<tr>
<td>n</td>
<td>number of particles to create.</td>
</tr>
<tr>
<td>draw</td>
<td>function to draw the particles, set from fdisplay[shape]</td>
</tr>
<tr>
<td>rotation</td>
<td>JSON value or 0, if not specified</td>
</tr>
<tr>
<td>image</td>
<td>reference to the loaded P5 image</td>
</tr>
<tr>
<td>length</td>
<td>number of active particles</td>
</tr>
<tr>
<td>left</td>
<td>number of particles still to create.</td>
</tr>
<tr>
<td>done</td>
<td>true if all particles have been created and deleted</td>
</tr>
</tbody>
</table>

**Sample fdisplay Function**

```javascript
function frect(fountain, particle) {
  fill(fountain.f.colors[int(particle.life*fountain.f.colors.length)]);
  noStroke();
  rect(particle.x, particle.y, particle.partSize, particle.partSize);
}

var fdisplay = {ellipse: fellipse, rect: frect, image: fimage};
```

**Definitions of Particle and Fountain and a JSON Fountain String**

http://jsfiddle.net/bobcook/2kfbmwtu/gz
Projectiles

The second utility class (Projectile) was designed for weapons of all types, which covers a lot of ground. There had to be lots of flexibility in bullet and projectile shapes. Luckily, flexibility is JavaScript's best feature. The design allows the user to define guns and their properties external to the class and to draw projectiles on demand external to the class. Further, projectiles must be physics bodies since they are required to have an impact upon collision.

The JSON evaluator for projectiles supports all of the Fountain properties except "sizePercent", which should be set to zero. New properties have been added for weapons and the physics of projectiles.

Each weapon has a load, which is the number of bullets per shot. The angle of a shot is the random spread in degrees around the shooting point. If the projectile load is one, the spread has a random effect on each shot. The period of a gun is the time that must elapse in milliseconds before it can be fired again. All bullets are particles so the speed property affects the velocity.

Remember that particles are not physics bodies. There are so many particles that modelling collisions would not really contribute anything to the "effect".

Bullets, however, are designed to hit things and to have an impact. Thus, all bullets are physics bodies. The following table lists the added JSON Projectile properties.

<table>
<thead>
<tr>
<th>Name</th>
<th>Description</th>
<th>Example</th>
</tr>
</thead>
<tbody>
<tr>
<td>sizePercent</td>
<td>not used. Set to zero.</td>
<td>&quot;sizePercent&quot;: 0</td>
</tr>
<tr>
<td>shape</td>
<td>string index into the fdisplay array to select a drawing function. The function must define the parameters body, shape, and position since it is a physics callback. Use the Fountain &quot;file&quot; property for images.</td>
<td>&quot;shape&quot;: &quot;pfill&quot;</td>
</tr>
<tr>
<td>gravity</td>
<td>sets the gravityScale of the physics body.</td>
<td>&quot;gravity&quot;: 1</td>
</tr>
<tr>
<td>angle</td>
<td>defines the spread of the projectile stream in degrees around the velocity vector.</td>
<td>&quot;angle&quot;: [-4, 4]</td>
</tr>
<tr>
<td>load</td>
<td>number of bullets per shot.</td>
<td>&quot;load&quot;: 5</td>
</tr>
<tr>
<td>period</td>
<td>number of milliseconds after a shot to reload.</td>
<td>&quot;period&quot;: 4000</td>
</tr>
<tr>
<td>pshape</td>
<td>physics shape: box, circle or polygon.</td>
<td>&quot;pshape&quot;: &quot;polygon&quot;</td>
</tr>
</tbody>
</table>

**Optional**

<table>
<thead>
<tr>
<th>Name</th>
<th>Description</th>
<th>Example</th>
</tr>
</thead>
<tbody>
<tr>
<td>density</td>
<td>density of the physics body.</td>
<td>&quot;density&quot;: 1</td>
</tr>
<tr>
<td>friction</td>
<td>friction of the physics body.</td>
<td>&quot;friction&quot;: 0.2</td>
</tr>
</tbody>
</table>
The Projectile example creates five physics box-bodies at random screen locations. When the mouse is clicked, twenty triangular projectiles are fired toward that location. Observe that the bullets have mass so when they hit a box, it moves proportional to the ratio of their masses. Any image can be defined as a projectile, i.e. flowers, ducks, bricks, etc. Also note that while the graphics is impressive, the code for the program is very simple.
var defs;
var of;

function setup() {
    createCanvas(600, 400);
    b2newWorld(30, createVector(0, 0));
    for (var i=0; i<5; i++)
        var b = new b2Body('box', true,
            createVector(random(50,550),random(50,350)),
            createVector(64,64));
    var t =
        '{  ' +
            ' "parts": [  ' +
                ' {  ' +
                    ' "name": "foo",  ' +
                    ' "color": "white","white","white","white"],  ' +
                    ' "shape": "pfill",  ' +
                    ' "pshape": "polygon",  ' +
                    ' "edges": [[5,5],[5,-5],[0,5]],  ' +
                    ' "gravity": 1,  ' +
                    ' "sizePercent": 0,  ' +
                    ' "angle": [-4,4],  ' +
                    ' "speed": 15.5,  ' +
                    ' "limit": 99999,  ' +
                    ' "lifetime": 60,  ' +
                    ' "size": [4,8],  ' +
                    ' "period": 1000,  ' +
                    ' "load": 20,  ' +
                    ' "rotation": 6,  ' +
                    ' "x": 2,  ' +
                    ' "y": 2 ]},
        ' };
defs = JSON.parse(t);
of = new Projectile(defs, 'foo');
}

function draw() {
    background(51);
b2Update();
b2Draw(false);
of.Step();
noStroke();
text(of.length, width/2, 20);
stroke(0);
}

//fire a shot toward the
//click location
function mousePressed() {
    of.Create(mouseX, mouseY);
}

**Projectile Class Definition** (inherits from Fountain)

<table>
<thead>
<tr>
<th>Methods</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>new</strong> Projectile(JSON table, name, x, y)</td>
</tr>
<tr>
<td>Create(x, y)</td>
</tr>
<tr>
<td>Function</td>
</tr>
<tr>
<td>--------------</td>
</tr>
<tr>
<td>Draw()</td>
</tr>
<tr>
<td>Step()</td>
</tr>
<tr>
<td>Stop()</td>
</tr>
</tbody>
</table>

Properties (includes Fountain)

<table>
<thead>
<tr>
<th>Property</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>fire</td>
<td>null or angle of fire from Create.</td>
</tr>
<tr>
<td>pedges</td>
<td>edge array converted to P5 vectors.</td>
</tr>
</tbody>
</table>

New Particle Property

<table>
<thead>
<tr>
<th>Property</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>body</td>
<td>reference to the physics body.</td>
</tr>
</tbody>
</table>

New b2Body Properties

<table>
<thead>
<tr>
<th>Property</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>fountain</td>
<td>references Fountain instance, used for drawing properties.</td>
</tr>
<tr>
<td>particle</td>
<td>references Particle instance, used in draw function.</td>
</tr>
</tbody>
</table>

Sample fdisplay Function

```javascript
function ffill(body, shape, position) {
    fill(body.fountain.f.colors[Math.floor(body.particle.life*body.fountain.f.colors.length)]);
    noStroke();
    b2Ddisplay(body, shape, position);
}
```

```javascript
var fdisplay = {pfill: ffill, ellipse: fellipse, rect: frect, image: fimage};
```

Finally, we discuss the implementation of the main program (using step-wise refinement, of course!). The first step is to identify the game components, then they can be implemented one step at a time.

Try to implement each step yourself before peeking at the Fiddle listing. (Expect many sessions with the FireFox debugger on any project.)

Game Components
<table>
<thead>
<tr>
<th><strong>Alien Ship</strong></th>
<th>A long triangle in the Fiddle, but an image in the PC version. Flies from a random left-side point towards a random right-side point. Should point in the direction of flight initially. Once a ship is destroyed, create another.</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>Score</strong></td>
<td>Displayed in the top-middle of the screen</td>
</tr>
<tr>
<td><strong>Star Field</strong></td>
<td>Move right-to-left and increases in size to enhance motion and distance &quot;feel&quot;. Created as a Fountain.</td>
</tr>
<tr>
<td><strong>Multiple Shot</strong></td>
<td>From earlier example. Shotgun projectile with 20 triangular bullets.</td>
</tr>
<tr>
<td><strong>Shield Buster</strong></td>
<td>Blue phason circle that penetrates a shield and destroys a ship. Requires collision detection with the ship, but not other bullets.</td>
</tr>
<tr>
<td><strong>Explosion</strong></td>
<td>Created as a Fountain at the point of ship destruction.</td>
</tr>
</tbody>
</table>

**Score**

The "score" variable is declared globally so that it can be accessed from any function. The score display is drawn using a text font. It took a bit of experimenting to choose a font and font size.

```javascript
var score = 0;
function draw() {
  background(51);
  textFont("Arial");
  textSize(40);
  fill(255);
  text("Score: " + score, width / 2 - 100, 50);
  stroke(0);
}
```
Alien Ship

The alien ship is a triangular physics object. A triangle must be drawn as a three-sided polygon. Remember that the points must be listed in counter-clockwise order.

The "ship" variable is also declared globally. We set the variable to null to indicate that a ship needs to be created. When a ship is destroyed, the variable is set to null. The next code written creates the ship and then applies an impulse to move it horizontally from left to right.

```javascript
var ship = null;
function draw() {
  background(51);
  if (ship == null) {
    var xy = createVector(2, width/2);
    var target = createVector(1, 0); // positive X direction
    var angle = 0;
    ship = new b2Body('polygon', true, xy, [createVector(0, 15), createVector(20, -40), createVector(-20, -40)], 1, 0.5, 0.2, angle);
    ship.applyImpulse(target, random(2, 8));
  }
}
```

Continuing, we need to add code to check if the ship has been knocked off the screen (+100) or if it has crossed the right edge (-100). The code was tested by launching the ship in different directions. The first bug was encountered at this point because the code did not handle the (height) case. The physics engine deactivates a body if it leaves the screen. The bug is fixed in the following code.

```javascript
var ship = null;
function draw() {
  background(51);
  if (ship == null) {
    var xy = createVector(2, width/2);
    var target = createVector(1, 0);
    var angle = 0;
    ship = new b2Body('polygon', true, xy, [createVector(0, 15), createVector(20, -40), createVector(-20, -40)], 1, 0.5, 0.2, angle);
    ship.applyImpulse(target, random(2, 8));
  } else {
    var xy = ship.xy;
    if (xy.x < 0 || xy.y < 0) {
      score += 100;
      ship.destroy();
      ship = null;
    }
  }
```
} else if (xy.x > width) {
    score -= 100;
    ship.destroy();
    ship = null;
} else ship.applyForce(ship.velocity, 0.03);
}
b2Update();
if (ship != null && !ship.active) { //off bottom case
    score += 100;
    ship = null;
}
b2Draw(false);
)

The remaining challenge is to fly the ship from a random left point to a random right point and to rotate the ship towards the target location. Given the two points, we need to calculate the velocity vector in order to apply the impulse properly. Further, given the (0, 1) initial orientation of the ship, the angle to rotate the nose must be calculated.

The velocity vector is just the vector-difference between the two points. However, the separation is hundreds of pixels, which is too large to use. Therefore, the result must be vector-normalized. Check out the Wikipedia article on Math.atan2. The function calculates the angle assuming that the gun is horizontal to start. In our case, the triangle needs to be rotated -90 degrees, or -PI/2 radians, to be horizontal.

```
var xy = createVector(2, random(height-30) + 10);
var target = createVector(width, random(height-30) + 10);
target.sub(xy);
var angle = -PI/2 + Math.atan2(target.y, target.x);
```

**Star Field**

The star field is created as a Fountain. I made the stars partially transparent to enhance the depth effect. I also created them small and then increased the size as they moved left. Because the definition was a JSON string, it was easy to experiment with different parameters. The hardest part was determining the points for a star shape. I found a star graphic on the Internet, downloaded it into a Paint program, enlarged the view, and then copied down the end points in a counter-clockwise direction. Remember that the "shape" name refers to a user-defined draw function in the "fdisplay" table.

The challenge in coding the star field was to generate the stars across the right side of the screen, not at a single point. Remember that the Fountain.Create function defines optional xy parameters. Aha!

st.Step();
st.Create(width-1, random(0, height));
Multiple Shot
Implement multiple shot projectiles only required copying the JSON definition from the Projectile test code. That code fired a shot in the direction of a mouse click so no change was needed there. However, there was a mysterious bug. Color names stopped working when using the physics library, so we just set the color to green by using the array notation \([0, 255, 0]\). We also had the set the "bullet" property to true as sometimes shots at an angle would "miss" collision detection.

Observe that the shots are powerful enough to knock a ship off course, but not powerful enough to penetrate the shields. At this point, we discovered that it was hard to beat the game!

**Shield Buster**

We added a "shield buster" projectile to give the player an additional advantage and to illustrate collision handling. Remember that the default collision category is one. A new category "4" was defined for the bullets and their "collidesWith" property was set to "4". Then we had to change the "categories" property of the ship to "4" and set its "collidesWith to "4+1". We also attached a "collision" function to the ship. These bullets are also fired towards a mouse click, but from a different location.

```javascript
function collider(bodyA, bodyB) {
  // test for ship and shield buster
  if (bodyA.categories == 4 && bodyB.categories == 4 && ship != null) {
    var xy = ship.xy;
    var x = new Fountain(defs, 'explosion', xy.x, xy.y);
    ex.push(x);
    ship.destroy();
    score += 100;
    ship = null;
  }
}

ship.categories = 4;
ship.collidesWith = 4 + 1;
ship.collision = collider;
```

```
  "name": "shieldBuster", 
  "color": [0,0,255], 
  "shape": "pfill", 
  "pshape": "circle", 
  "gravity": 1, 
  "sizePercent": 0, 
  "angle": [0,0], 
  "speed": 50, 
  "limit": 99999, 
  "lifetime": 80,
```
Explosion

The explosion that occurs upon ship destruction is also defined as a Fountain. I had to experiment with the parameters to get a reasonable "look". The challenge with this final component was that multiple explosions could be active simultaneously. As a result, the code had to create particles for all active explosions and to delete explosions that had terminated.

The solution was to declare an array "ex" to store active explosions. Remember that the Fountain class defines a "done" property, which can be checked to determine a Fountain's completion status. Also, remember that the Fountain constructor has optional xy parameters that can be set to locate particle streams.

```javascript
var ex = [];

for (var i = 0; i < ex.length; i++) {
    ex[i].Step();
    ex[i].Create();
    ex[i].Draw();
    if (ex[i].done) ex.splice(i, 1);
}
```

Final Result
M.I.T. Software License

Permission is hereby granted, free of charge, to any person obtaining a copy of this software and associated documentation files (the "Software"), to deal in the Software without restriction, including without limitation the rights to use, copy, modify, merge, publish, distribute, sublicense, and/or sell copies of the Software, and to permit persons to whom the Software is furnished to do so, subject to the following conditions:

The above copyright notice and this permission notice shall be included in all copies or substantial portions of the Software.

THE SOFTWARE IS PROVIDED "AS IS", WITHOUT WARRANTY OF ANY KIND, EXPRESS OR IMPLIED, INCLUDING BUT NOT LIMITED TO THE WARRANTIES OF MERCHANTABILITY, FITNESS FOR A PARTICULAR PURPOSE AND NONINFRINGEMENT. IN NO EVENT SHALL THE AUTHORS OR COPYRIGHT HOLDERS BE LIABLE FOR ANY CLAIM, DAMAGES OR OTHER LIABILITY, WHETHER IN AN ACTION OF CONTRACT, TORT OR OTHERWISE, ARISING FROM, OUT OF OR IN CONNECTION WITH THE SOFTWARE OR THE USE OR OTHER DEALINGS IN THE SOFTWARE.